## 6.2.6 Coefficients of Variation

Sampling errors are estimated in terms of coefficient of variation, CV (%), according to the following relationships:

In each stratum h, the following can be defined:

 $N_h$ : the population size

 $n_h$ : the sample size

 $m_h$ : the number of responding units

 $\mathcal{W}_{bi}$  : the extrapolation factor of the agricultural holding of order i belonging to stratum h

 $\boldsymbol{y}_{\scriptscriptstyle hi}$  : the value of the survey characteristic y of the holding of order i ,

 $\boldsymbol{Y}_{\scriptscriptstyle h}$  : the sum of the values of the characteristic y of all holdings in the stratum

Y : the sum of the values of the characteristic y of all holdings in all strata

That is: 
$$Y = \sum_{h} Y_{hi}$$

The estimations of the magnitudes  $oldsymbol{Y}_{\scriptscriptstyle h}$  and Y come from the following relations:

$$\widehat{Y}_h = \sum_{i=1}^{n_h} \mathcal{W}_{hi} \cdot \mathcal{Y}_{hi}$$

$$\widehat{Y} = \sum_{h} \widehat{Y}_{h} = \sum_{h} \sum_{i} W_{hi} \cdot Y_{hi}$$

The estimations of the variances for  $\hat{Y}_h$  and  $\hat{Y}$  are calculated using the following relations:

$$V(\widehat{Y}_h) = \frac{N_h(N_h - m_h)}{m_h} S_h^2 \quad \text{where: } S_h^2 = \frac{1}{m_h - 1} \left[ \sum_{i=1}^{m_h} y_{hi}^2 - \frac{(\sum_{i=1}^{m_h} y_{hi})^2}{m_h} \right]$$

$$V(\widehat{Y}) = \sum_{h} V(\widehat{Y}_{h})$$

The coefficient of variation (%) of the  $\hat{Y}$  is given by the following relation:

$$CV(\widehat{Y}) = \frac{\sqrt{V(\widehat{Y})}}{\widehat{Y}} \cdot 100$$