

### 18.1.2 Sampling design

The sampling design is a probability design (multi-stage stratified sampling).

**Number of individuals interviewed in the selected household:** One individual

**Number of sampling stages:** Two stages for households and three stages for individuals.

The primary sampling units are areas (one or more unified city blocks) participating in the EU-SILC of the years 2016 – 2022.

#### 1) First stage – Stratification

The stratification variables of the first stage units (one or more unified city blocks) are:

1. Region (NUTS 2)
2. Degree of urbanization.

In each Region (NUTS 2), the stratification of primary units (first stage units) was conducted by allocating the Communes according to the degree of urbanization. Except for the former two Major City Agglomerations (Athens and Thessaloniki), the strata according to the degree of urbanization are:

1. Communes with 30.000 inhabitants or more
2. Communes with 5.000 to 29999 inhabitants
3. Communes with 1.000 to 4.999 inhabitants
4. Communes up to 999 inhabitants

The former Greater Athens Area was divided into 31 strata of about equal size (equal number of households), on the basis of lists of city blocks of the Communes that constitute it and taking into consideration socio-economic criteria. Similarly, the former Greater Thessaloniki Area was divided into 9 equally sized strata. Thus, the total number of strata of the survey was 90, that is the 'final strata'.

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#### **1<sup>st</sup> stage of sampling**

In this stage, for any ultimate stratum ('final strata'), say stratum  $h$ ,  $a_h$  primary units were drawn with probabilities proportional to their sizes. The number  $a_h$  of draws is approximately proportional to the population stratum size  $N_h$ , as defined above.

The primary unit of order  $i$  in stratum  $h$  has probability of being drawn proportional to the population size as follows:

$$P_{hi} = \frac{a_h \cdot N_{hi}}{N_h} \quad (1)$$

where:

$N_{hi}$  : Updated number of households from the EU-SILC in the  $hi$  primary unit.

$N_h$  : Estimated number of households for the year 2021 in the stratum  $h$ .

The secondary sampling units are the households of the EU-SILC containing members belonging to the target population (individuals aged 16-74 years old). The third –and final– sampling unit is one person randomly selected among the household members of 16-74 years old.

In more detail:

### **2<sup>nd</sup> stage of sampling**

In the  $hi$  primary unit, a sample of  $n_{hi}$  out of  $N_{hi}$  households was selected with equal probabilities. Each one of the  $n_{hi}$  households had the same chance to be selected, equal to:

$$\frac{n_{hi}}{N_{hi}} \quad (2)$$

The total number of households to be interviewed of the  $a_h$  sampling primary units is:

$$n_h = \sum_{i=1}^{a_h} n_{hi}$$

Within each primary sampling unit the calculation of the sampling interval  $\delta_{hi} = \frac{N_{hi}}{n_{hi}}$  was carried out, so that the following two desired conditions to be satisfied.

a) The expectation of the fraction  $\frac{n_h}{N_h}$  was constant in each stratum. That is:

$$E\left(\frac{n_h}{N_h}\right) = \frac{1}{\lambda} = 2.96\% \quad (3) \quad \text{and}$$

b) The estimator of the stratum total  $Y_h$  (for any characteristic) will be self-weighting. In other words, the estimate of the survey characteristics is derived as product of the sum of the values of the characteristics over the  $n_h$  sample households by the overall raising factor  $\lambda$ , which is equal in each stratum.

The conditions (a) and (b) are satisfied when:

$$\frac{1}{a_h} \cdot \frac{1}{P_{hi}} \cdot \frac{N_{hi}}{n_{hi}} = \lambda \quad (4) \Rightarrow \frac{1}{a_h} \cdot \frac{1}{P_{hi}} \cdot \delta_{hi} = \lambda \Rightarrow \delta_{hi} = \frac{N_{hi}}{n_{hi}} = \lambda \cdot a_h \cdot P_{hi} \quad (5)$$

From the relations (1) and (5)  $\Rightarrow$

$$\frac{N_{hi}}{n_{hi}} = \lambda \cdot a_h \cdot \frac{N_{hi}}{N_h} \Rightarrow n_{hi} = \frac{N_{hi} \cdot N_h}{\lambda \cdot a_h \cdot N_{hi}} \Rightarrow n_{hi} = \frac{N_h}{\lambda \cdot a_h} \quad (6)$$

From the relation (3), it is deducted that:  $\frac{1}{\lambda} = \frac{n_h}{N_h} \Rightarrow \lambda = \frac{N_h}{n_h} \quad (7)$

From the relations (6) and (7), we have:  $n_{hi} = \frac{n_h}{a_h} \quad (8)$

### **3<sup>rd</sup> stage of sampling**

In this stage from each household one individual (member of household belonging to the target population) was selected with equal probabilities.

Let  $p_{hij}$  is the selection probability of the  $hij$  individual, which belongs to the  $hi$  household.

As one individual was selected with equal probabilities out of  $m_{hi}$  members belonging to target population, the  $p_{hij}$  was defined as:  $p_{hij} = \frac{1}{m_{hi}}$

The sampling fraction in each of the 90 strata (Stratum= Region x Degree of urbanization) is

$f = \frac{1}{\lambda} = \frac{n}{N} \cong 0.0029$  where  $n=10,992$  is the total sample size of households and  $N=3,711,296$  is the estimated total number of households belonging to the target population.

The number of the sampling households in each of the 90 strata (let  $h$ ) was defined by applying the proportional allocation as follows:

$$n_h = n \cdot \frac{N_h}{N}$$

where:

$N_h$ : the population size of the stratum  $h$ .