The Maturity Structure of Debt, Monetary Policy and Expectations Stabilization

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- 'Standard' view of monetary policy
 - Monetary authority alone determines inflation
 - Fiscal authority guarantees intertemporal solvency of the government
 - Expectations are 'anchored': consistent with policy objectives

- Alternative views: 'Unpleasant arithmetic' and Fiscal theory of the price level
 - Outstanding nominal liabilities not fully backed up by future taxes
 - "Nominal anchor" shifts to fiscal policy

- This presentation:
 - Incomplete knowledge about policy regime
 - Expectations inconsistent with policy objectives
 - Nonricardian effects regardless of the policy regime

What we do

- Simple NK model of output gap and inflation determination
- Departure from rational expectations:
 - Agents have an incomplete knowledge about the economy: learning
 - Implication: departures from Ricardian Equivalence
- Explore constraints imposed on monetary policy by choice of fiscal policy
 - Specifically: scale and composition of government debt

Results

• High level of debt...

• ...and short to medium maturity debt can lead to unanchored expectations

• Instability occurs if wealth effects from holding government debt are sufficiently strong

Model

Model Agents

- Households
- Firms
- Monetary authority
- Fiscal authority

Maturity of Public Debt

• Issues two kinds of debt

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– B_t^m : An asset in positive supply that has declining payoff structure

$$\rho^{T-(t+1)}$$
 for $T \ge t+1$

- P_t^m denotes the price of this second asset.
- Duration of the debt is $(1 \beta \rho)^{-1}$; β discount rate

• Flow budget constraint

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• Fiscal policy maintains intertemporal solvency ('Passive')

$$\tau_t^i = \bar{\tau}^i \left(\frac{B_{t-1}^m}{\bar{B}^m} \right)^{\tau_l^i}$$
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• Monetary policy controls inflation ('Active')

$$\frac{1+i_t}{1+\overline{\imath}} = \left(\frac{\pi_t}{\pi^*}\right)^{\phi_\pi}; \quad \phi_\pi > 1$$

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• Under rational expectations: standard view of monetary policy

Household Problem

- Saving and work decision. No capital in the model, only gov. bonds.
- Households' preferences

$$U(C_t, H_t) = (1 - \sigma)^{-1} \left(C_t - \frac{\psi}{1 + \gamma} C_t^{\prime} H_t^{1 + \gamma} \right)^{1 - \sigma}, \gamma > 0$$

where

- $\iota = \mathbf{0} \rightarrow GHH$; $\iota = \mathbf{1} \rightarrow KPR$ preferences

 $-\sigma \geq 1 \rightarrow IES \leq 1, C_t, H_t$ complements

Key Equation 1: Consumption Decision

• Combining Euler eqs., labor supply, budget constraint to log-linear approx. provides

$$\hat{C}_t^{(i)} - (1 - \sigma^{-\iota})\Theta\hat{H}_t^{(i)} = \bar{s}_C^{-1}(\sigma, \iota) \left(\frac{S}{\bar{Y}}\right) \times$$

$$\times \underbrace{\left(\hat{b}_{t-1}^{m,(i)} - \hat{\pi}_t + \rho\beta\hat{P}_t^m - \hat{E}_t^{(i)}\sum_{T=t}^{\infty}\beta^{T-t}\left[T(\hat{\tau}_T^{LS}, \hat{\tau}_T^W) - \beta\left(\hat{\imath}_T - \hat{\pi}_{T+1}\right)\right]\right)}_{C}$$

$$+\overline{s}_{C}^{-1}(\sigma,\iota)\left(1-\beta\right)\hat{E}_{t}^{(i)}\sum_{T=t}^{\infty}\beta^{T-t}x\left(\hat{w}_{T},\hat{\Gamma}_{T}\right)-\beta\sigma^{-1}\hat{E}_{t}^{(i)}\sum_{T=t}^{\infty}\beta^{T-t}\left(\hat{\imath}_{T}-\hat{\pi}_{T+1}\right)$$

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Key Equation 2: Public Debt

• Price of government debt

$$\hat{P}_{t}^{m} = \underbrace{-\hat{E}_{t}\sum_{T=t}^{\infty} (\rho\beta)^{T-t} \hat{\imath}_{T}}_{\text{Expectation Hypothesis}}$$

• Evolution of public Debt

$$\hat{b}_{t}^{m} = \beta^{-1} \left(\hat{b}_{t-1}^{m} - \hat{\pi}_{t} \right) + (1 - \rho) \hat{\imath}_{t} - \left(\beta^{-1} - 1 \right) \hat{s}_{t}$$
$$+ (1 - \rho) \rho \beta \hat{E}_{t} \sum_{T=t}^{\infty} (\rho \beta)^{T-t} \hat{\imath}_{T+1}$$

Firms

• Monopolistic competition + nominal rigidities (Rotemberg)

• In aggregate, the Phillips curve

$$\hat{\pi}_t = \psi \left(\gamma + \frac{\bar{Y}}{\bar{C}} \iota \right) \hat{Y}_t +$$

$$+\hat{E}_t\sum_{T=t}^{\infty} (\alpha\beta)^{T-t} \left[\psi\alpha\beta\hat{w}_{T+1} + (1-\alpha)\beta\hat{\pi}_{T+1}\right]$$

Knowledge and learning

- Agents know only their own preferences and constraints
 - Simple model: agents are in fact identical but not aware of it

• Observe aggregate variables and disturbances

- Do not know true economic model determining variables outside their control
 - Forecasts using an econometric model
 - Model of anticipated utility: optimization ignores future model revisions

Learning and Expectations

• Inflation as an example. Rational Expectations (RE)

$$\hat{E}^{RE}_t \pi_{T+1} = \mathbf{0} + \mathbf{\Omega}^{RE}_b \hat{b}^m_{t-1}$$
, where $T > t$

• Learning

$$\hat{E}_t \pi_{T+1} = \mathbf{\Omega}_{c,t-1}^L + \mathbf{\Omega}_{b,t-1}^L \hat{b}_{t-1}^m + \text{lagged variables},$$

- Coefficients updated every period (Recursive Least Squares)
- Convergence to RE? E-stability
 - Use methods of Marcet and Sargent (1989), Evans and Honkapohja (2001)

E-stability

- Numerical study: LUMP SUM taxation
- Key parameters: $\sigma^{-1} = 1/4$, and $\frac{\bar{P}^m \bar{B}^m}{4\bar{P}\bar{Y}} = 1.5$
- Others:
 - Preferences and technology: $\beta = 0.99$, $\alpha = 0.8$ (Price stickiness)
 - Fiscal Policy: $au_l^{LS} = 1.5$
 - Steady State: $\bar{C}/\bar{Y} = 0.78$:



INTUITION

• Ricardian Households

$$\hat{C}_t - (1 - \sigma^{-\iota})\Theta\hat{H}_t =$$

$$-\beta \sigma^{-1} \hat{E}_t^i \sum_{T=t}^{\infty} \beta^{T-t} \left(\phi_\pi \hat{\pi}_T - \hat{\pi}_{T+1} \right) +$$

$$+\overline{s}_C^{-1}(\sigma,\iota)\hat{E}_t^i\sum_{T=t}^{\infty}\beta^{T-t}x_T$$

– we have substituted for the bond price equation and the monetary policy rule, $\hat{\imath}_t = \phi_\pi \hat{\pi}_t$

• Baseline

$$\hat{C}_t - (1 - \sigma^{-\iota})\Theta \hat{H}_t =$$

$$-\beta \left(\sigma^{-1} - \bar{s}_C^{-1}(\sigma, \iota) \frac{\bar{S}}{\bar{Y}} \right) \hat{E}_t^i \sum_{T=t}^{\infty} \beta^{T-t} \left(\phi_\pi \hat{\pi}_T - \hat{\pi}_{T+1} \right) +$$

$$-\bar{s}_C^{-1}(\sigma,\iota)\frac{\bar{S}}{\bar{Y}}\cdot\beta\rho\hat{E}_t\sum_{T=t}^{\infty}\left(\beta\rho\right)^{T-t}\left(\phi_{\pi}\hat{\pi}_T\right)+$$

$$+\overline{s}_C^{-1}(\sigma,\iota)\frac{\overline{S}}{\overline{Y}}\hat{b}_{t-1}^m + \overline{s}_C^{-1}(\sigma,\iota)(1-\beta)\hat{E}_t^i\sum_{T=t}^{\infty}\beta^{T-t}[x_T-T_T].$$

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Gov. Debt: Increase in Inflation Expectations

• Using the bond price equation and the monetary policy rule, $\hat{\imath}_t = \phi_{\pi} \hat{\pi}_t$, permits the evolution of real debt to be written as

$$\hat{b}_{t}^{m} = \beta^{-1} \left(\hat{b}_{t-1}^{m} - \hat{\pi}_{t} \right) + (1 - \rho) \phi_{\pi} \hat{\pi}_{t} - \left(\beta^{-1} - 1 \right) \hat{s}_{t} + (1 - \rho) \rho \beta \hat{E}_{t} \sum_{T=t}^{\infty} (\rho \beta)^{T-t} \phi_{\pi} \hat{\pi}_{T+1}$$

which depends on the maturity structure

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which depends on the maturity structure through

$$(1-\rho)\rho\beta\hat{E}_t\sum_{T=t}^{\infty}(\rho\beta)^{T-t}\phi_{\pi}\hat{\pi}_{T+1} = \frac{(1-\rho)\rho\beta}{1-\rho\beta}\phi_{\pi}\hat{E}_t\pi$$

– For $\beta = 0.99$ the right hand side peaks $ho \simeq 0.9$: average maturity of 2 years

- For $\rho = 1$: infinite maturity debt dynamics independent of its own price.

IES and Debt-to-Output Ratio



 σ





Forward-looking policy rules

• Alternative policy rules that responds to expectations

$$\hat{\imath}_t = \phi_\pi \hat{E}_t \hat{\pi}_{t+1}$$

• Here we assume that agents know the policy rule



Intuition: Debt Dynamics

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- Debt depends on expectations regardless of ρ
- Destabilizing effects on consumption and debt decline monotonically with ρ

Distortionary taxation

- Consider the model labor taxes (au_t^w) ...
- ...and assume now: $\sigma^{-1} = 1/2$



Intuition: Distortionary taxation

- Same mechanism as before but with a 'twist'
- Phillips curve has an extra term

$$\hat{\pi}_{t} = \psi \left[\left(\gamma + \frac{\bar{Y}}{\bar{C}} \iota \right) \hat{Y}_{t} + \frac{\bar{\tau}^{w}}{(1 - \bar{\tau}^{w})} \hat{\tau}_{t}^{w} \right] + \hat{E}_{t} \sum_{T=t}^{\infty} (\alpha \beta)^{T-t} \left[\psi \alpha \beta \hat{w}_{T+1} + (1 - \alpha) \beta \hat{\pi}_{T+1} \right]$$

• Changes in tax rates as cost-push "shocks", reinforcing the drift in expectations

Conclusion

- Uncertainty about policy regime can induce drift in expectations
- High debt levels and short to medium maturity debt induce instability
 - Instability generated through wealth effects
- Fundamentally changes the nature of household and firm responses to shocks even if expectations stable in the long-run
- In such a world fiscal communication stabilizing