

ESTIMATING SOVEREIGN DEFAULT RISK

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WHERE WE ARE TODAY

TABLE 1: 10-yr Nominal Interest Rate Spread (against Germany)

	2010	2011
Italy	1.65	5.19
Greece	8.99	16.05

WHERE WE ARE TODAY

- Theory
 - Ability to service debt is country specific
 - Rational expectations → default probabilities forward looking
 - e.g. Bi (2011), Juessen, et al (2011)

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- Theory
 - Ability to service debt is country specific
 - Rational expectations → default probabilities forward looking
 - e.g. Bi (2011), Juessen, et al (2011)
- Empirical
 - Panel regressions, e.g. Alesina, et al (1992)
 - Backward looking debt limits, e.g. Ostry, et al (2010)

THIS PAPER

- Estimate RBC model of sovereign default
- Use Bayesian methods; Italian and Greek post-EMU data
- Main Results
 - For given debt level, Greece had lower default probability
 - Italy more willing to service debt than Greece

MODEL

- RBC, closed economy model
- Fiscal instruments: spending, taxes, transfers, debt
- Endogenous probability of sovereign (partial) default

MODEL: HOUSEHOLDS

Preferences:

$$E_0 \sum_{t=0}^{\infty} \beta^t \{ \log(c_t - h\bar{c}_{t-1}) + \phi \log(1 - n_t) \}$$

Budget constraint:

$$(1 - \tau_t)A_t n_t + z_t - c_t = \frac{b_t}{R_t} - (1 - \Delta_t)b_{t-1}$$

$$A_t - A = \rho_A(A_{t-1} - A) + \epsilon_t^A. \quad \epsilon_t^A \sim \mathcal{N}(0, \sigma_A^2)$$

MODEL: GOVERNMENT

- Government budget constraint:

$$\tau_t A_t n_t + \frac{b_t}{R_t} = g_t + z_t + \underbrace{(1 - \Delta_t) b_{t-1}}_{b_{t-1}^d}$$

- Fiscal Rules:

$$g_t - g = \rho_g (g_{t-1} - g) - \gamma_g (b_{t-1}^d - b) + \epsilon_t^g, \quad \epsilon_t^g \sim \mathcal{N}(0, \sigma_g^2)$$

$$\tau_t - \tau = \rho_\tau (\tau_{t-1} - \tau) + \gamma_\tau (b_{t-1}^d - b) + \epsilon_t^\tau, \quad \epsilon_t^\tau \sim \mathcal{N}(0, \sigma_\tau^2)$$

$$z_t - z = \rho_z (z_{t-1} - z) + \epsilon_t^z, \quad \epsilon_t^z \sim \mathcal{N}(0, \sigma_z^2)$$

MODEL: GOVERNMENT

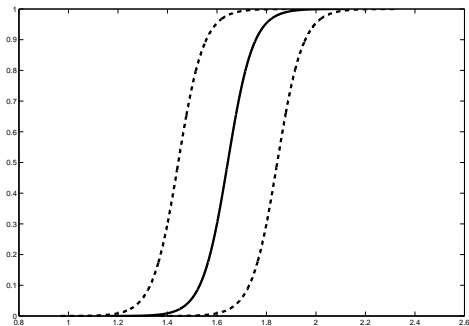
- Effective, stochastic fiscal limit b_t^* implying default scheme:

$$\Delta_t = \begin{cases} 0 & \text{if } b_{t-1} < b_t^* \\ \delta & \text{if } b_{t-1} \geq b_t^* \end{cases}$$

- b_t^* related to
 - Dynamic tax Laffer curve
 - Political willingness to finance debt
- b_t^* drawn from Logistic distribution

MODEL: FISCAL LIMIT

- Estimate point: $P(\tilde{b}^* \geq b) = 0.3$
- Assume $\hat{b}^* - \tilde{b}^* = 0.4$, where $P(\hat{b}^* \geq b) = 0.999$
- Prior: $\tilde{b}^* \sim U(1.4, 1.8)$



EQUILIBRIUM

Competitive equilibrium:

- HH maximize utility subject to budget
- Gov. policy satisfies its budget
- Markets clear, implying

$$c_t + g_t = A_t n_t$$

ESTIMATION

- Italy (1999:2-2010:3) and Greece (2001:2-2010:3)
- Observables: y, g, T, b, R
- Assume measurement error
- Priors: standard in literature

SOLVING MODEL

- Use monotone mapping method
 - Coleman (1991), Davig (2004)
 - Discretize state space
 - Iterate on policy functions

ESTIMATING MODEL

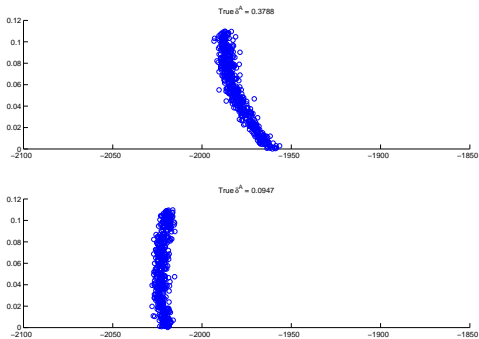
- Sequential Monte Carlo approximation of likelihood [Doh (2011)]
 - Initialize state x_0 with N particles
 - Drawn N particles $u^{t|t-1,i}$
 - Construct $x^{t|t-1,i}$ and assign weight

$$w_t^i = \frac{1}{(2\pi)^{5/2} |\Sigma|^{1/2}} \exp \left[-\frac{1}{2} \left(y_t - Ax^{t|t-1,i} \right)' \Sigma \left(y_t - Ax^{t|t-1,i} \right) \right]$$

- Normalize weights & resample w/ replacement
 - Log-likelihood approximation: $\sum_{t=1}^T \ln \left(\frac{1}{N} \sum_{i=1}^N w_t^i \right)$
- Posterior distribution from Metropolis-Hastings algorithm

ESTIMATING MODEL

- Identifiability of parameters



- Calibrate $\delta = \{0.0978, 0.05, 0.0245\}$

CALIBRATED PARAMETERS

	Italy	Greece
β	0.99	0.99
\bar{n}	0.75	0.75
\bar{g}/\bar{y}	0.1966	0.1795
\bar{b}/\bar{y}	1.19*4	1.14*4
τ	0.4148	0.3387

- Estimated parameters: \tilde{b}^* , h , γ^g , γ^r , ρ^a , ρ^z , ρ^g , ρ^r , σ_a , σ_g , σ_τ , σ_z

ESTIMATES FOR ITALY

	Prior	$\delta^A = 0.3788$
\tilde{b}^*	1.60 [1.42, 1.78]	1.52 [1.46, 1.60]
$\gamma^{g,L}$	0.40 [0.12, 0.82]	0.30 [0.16, 0.56]
$\gamma^{\tau,L}$	1.1 [0.64, 1.67]	0.53 [0.45, 0.66]

- \tilde{b}^* informed from data

ESTIMATES FOR ITALY

	Prior	$\delta^A = \mathbf{0.3788}$	$\delta^A = \mathbf{0.2}$
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$\gamma^{g,L}$	0.40 [0.12, 0.82]	0.30 [0.16, 0.56]	0.59 [0.17, 0.82]
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- $\downarrow \delta \implies \downarrow \tilde{b}^*$

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- **Low δ calibration $\implies \tilde{b}^*$ not well-identified**

ESTIMATES FOR GREECE

	Prior	$\delta^A = \mathbf{0.0978}$
\tilde{b}^*	1.60 [1.42, 1.78]	1.45 [1.40, 1.57]
$\gamma^{g,L}$	1.1 [0.64, 1.67]	1.51 [1.08, 1.78]
$\gamma^{\tau,L}$	1.1 [0.64, 1.67]	1.14 [0.94, 1.48]

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ESTIMATES FOR GREECE

	Prior	$\delta^A = \mathbf{0.2}$	$\delta^A = \mathbf{0.0978}$
\tilde{b}^*	1.60 [1.42, 1.78]	1.69 [1.57, 1.79]	1.45 [1.40, 1.57]
$\gamma^{g,L}$	1.1 [0.64, 1.67]	1.53 [1.22, 1.85]	1.51 [1.08, 1.78]
$\gamma^{\tau,L}$	1.1 [0.64, 1.67]	0.76 [0.46, 1.00]	1.14 [0.94, 1.48]

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- $\downarrow \delta^A \implies \downarrow \tilde{b}^*$

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	Prior	$\delta^A = \mathbf{0.3788}$	$\delta^A = \mathbf{0.2}$
\tilde{b}^*	1.60 [1.42, 1.78]	1.67 [1.58, 1.78]	1.69 [1.57, 1.79]
$\gamma^{g,L}$	1.1 [0.64, 1.67]	1.73 [0.87, 2.97]	1.53 [1.22, 1.85]
$\gamma^{\tau,L}$	1.1 [0.64, 1.67]	0.82 [0.54, 1.09]	0.76 [0.46, 1.00]

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- \tilde{b}^* same for high/mid δ^A , γ 's adjust

ESTIMATED FISCAL LIMIT

- How close is estimated fiscal limit to maximum serviceable debt implied by model?

LAFFER CURVE & FISCAL LIMIT

- τ_t^{max} : tax rate at Laffer curve peak
- T_t^{max} : tax revenue at Laffer curve peak
- Maximum debt level in model:

$$\mathcal{B}^{max} = E \sum_{t=0}^{\infty} \beta^{t+1} \frac{u_c^{max}(A_{t+1}, g_{t+1})}{u_c^{max}(A_0, g_0)} (T^{max}(A_t, g_t) - g_t - z_t)$$

FISCAL LIMIT IN PRACTICE

- Political obstacles to achieve tax peak
- Reduced-form political economy representation
- Introduce “political factor” β^{pol} :

$$\mathcal{B}^* = E \sum_{t=0}^{\infty} \beta^{t+1} \beta^{pol} \frac{u_c^{max}(A_{t+1}, g_{t+1})}{u_c^{max}(A_0, g_0)} (T^{max}(A_t, g_t) - g_t - z_t)$$

- Ratio of \tilde{b}^{max} to \tilde{b}^* is political factor estimate

FISCAL LIMIT IN ITALY

	$\delta^A = 0.3788$		$\delta^A = 0.0947$	
	median	[5, 95]	median	[5, 95]
\tilde{b}^{max}	2.45	[2.38, 2.49]	2.47	[2.24, 2.51]
\tilde{b}^*	1.52	[1.46, 1.6]	1.6	[1.44, 1.78]
β^{pol}	0.62	[0.59, 0.67]	0.65	[0.58, 0.73]

FISCAL LIMIT IN

GREECE

	$\delta^A = 0.3788$		$\delta^A = 0.0947$	
	median	[5, 95]	median	[5, 95]
\tilde{b}^{max}	3.32	[3.15, 3.36]	3.26	[3.07, 3.35]
\tilde{b}^*	1.67	[1.58, 1.78]	1.45	[1.40, 1.57]
β^{pol}	0.5	[0.48, 0.54]	0.45	[0.42, 0.48]

FISCAL LIMIT IN ITALY/GREECE

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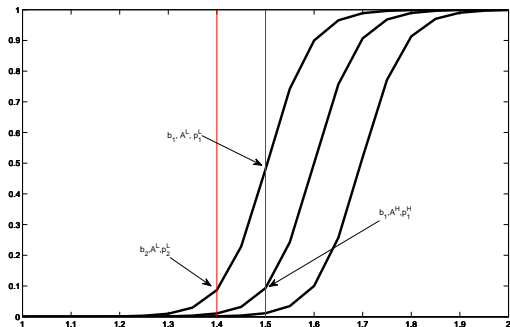
β^{pol} : Italy	0.62	0.65
β^{pol} : Greece	0.5	0.45

EXTENSION: STATE DEPENDENT FISCAL LIMIT

- Issue: Model has difficulty w/ recent recession

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- Issue: Model has difficulty w/ recent recession
- Stochastic fiscal limit drawn from conditional distribution, $b_t^* \sim \mathcal{B}^*(A_{t-1})$
- $P(b_{t-1} \geq b^*) = \frac{\eta_3 \exp(\eta_1 + \eta_2 b_{t-1} + \eta_5 A_{t-1})}{\eta_4 + \exp(\eta_1 + \eta_2 b_{t-1} + \eta_5 A_{t-1})}$



CONCLUSION

- Show how to estimate DSGE model of sovereign default
- For given debt level, Greece had lower default probability
- Italy more willing to service debt than Greece

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- Ongoing research:
 - Estimate model with broader set of Eurozone countries
 - Incorporate state dependence in fiscal limit